

for  $y$ -intersection put  $x=0 \Rightarrow y=1/0$   
 $\Rightarrow$  fix cuts  $y$ -intercept at  $(0, 1/0)$

Q.  $y = (x-1)(x-2)$  sketch the curve.

Soln  $= x^2 - 3x + 2$  ①

Step 1 find the intercepts with the co-ordinates axis  $y$ -intercepts is obtained by setting  $x=0$  and  $x$ -intercepts are the real roots of the eqn put  $f(x) = 0 = y$

$\Rightarrow$  put  $x=0$  in eqn ① we get  $y = (0-1)(0-2)$   
 $\Rightarrow y = 2$

put  $y=0$  in eqn ① we get  $(x-1)(x-2) = 0$   
 $\Rightarrow x = 1, 2$

$\Rightarrow$  curve intersect at  $x$ -axis at  $x=1, 2$   
 $\&$  intersect at  $y$ -axis at  $y=2$

Step (2), (3) find  $f'(x)$ ,  $f''(x)$  and critical pts

$$f'(x) = 2x - 3$$

$$\text{critical pt} \Rightarrow f'(x) = 0 \Rightarrow x = 3/2$$

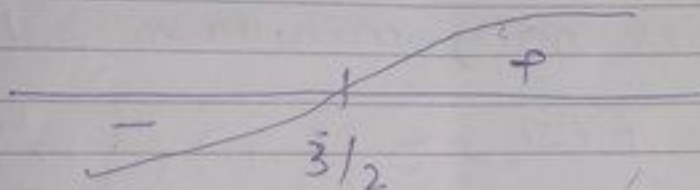
$$f''(x) = 2 > 0$$

Step (4) find the interval in which  $f^n$  is increasing and decreasing.

$$f'(x) = 2x - 3 = g(x)$$

$g(x) = 2x - 3$  check the behavior of  $f^n$  where  $g(x) > 0$  or  $g(x) < 0$

$$\text{Now } g(x) = 0 \Rightarrow 2x - 3 = 0 \quad x = 3/2$$



$$g(x) > 0 \text{ on } x \in (3/2, \infty) \Rightarrow g(x) = f'(x) > 0 \text{ on } x \in (3/2, \infty)$$

$$g(x) < 0 \text{ on } x \in (-\infty, 3/2) \Rightarrow g(x) = f'(x) < 0 \text{ on } x \in (-\infty, 3/2)$$

$$\Rightarrow f'(x) > 0 \text{ on } x \in (3/2, \infty) \Rightarrow f^n \text{ is increasing on } (3/2, \infty)$$

$$\therefore f'(x) < 0 \text{ on } x \in (-\infty, 3/2) \Rightarrow f^n \text{ is decreasing on } (-\infty, 3/2)$$

Step (5) Identify any points of inflection  
 $\therefore f''(x) = 2 \neq 0 > 0 \Rightarrow$  no point of inflection

Step 6 find the interval on which the fn is concave up or concave down

$$\therefore f''(x) = 2 > 0 \Rightarrow \text{fn is concave up } \forall x$$

Step 7 find the maximum and minimum values of the fn if exist

$$\therefore f'(x) = 2x - 3 \quad \& \quad f'(x) = 0 \Rightarrow x = 3/2$$

$$f''(x) = 2 > 0 \quad \text{on } \mathbb{R} \Rightarrow f''(3/2) = 2 > 0$$

$\Rightarrow$  fn has only minimum value

$$f(3/2) = \left(\frac{3}{2} + 1\right) \left(\frac{3}{2} - 2\right)$$

$$= \left(\frac{3-2}{2}\right) \left(\frac{3-4}{2}\right) = \frac{1}{2} \times -\frac{1}{2}$$

$$f(3/2) = -\frac{1}{4} \quad \text{minimum value of fn at } x = 3/2$$

fn has no maximum value

Step 8 Identifying asymptote

for horizontal asymptote a line  $y = b$  is a horizontal asymptote of graph  $f$  if

$$\lim_{x \rightarrow \infty} f(x) = b \quad \text{or} \quad \lim_{x \rightarrow -\infty} f(x) = b$$

$b = \text{must be finite}$

→ in this fn  $y = x^2 - 3x + 2$  there is no finite value  $y = b$  s.t  
 $\lim_{x \rightarrow \infty} f(x) = b$  or  $\lim_{x \rightarrow -\infty} f(x) = b$

⇒ no horizontal asymptote

→ for vertical asymptote: A line  $x = a$  is vertical asymptote of the graph  $f(x)$  if either sided limit

$\lim_{x \rightarrow a^-} f(x) \Rightarrow \infty$  or  $\lim_{x \rightarrow a^+} f(x) \Rightarrow \infty$

Here  $y = x^2 - 3x + 2$  there is no value of  $x = a$  (finite) s.t  
 $\lim_{x \rightarrow a^-} f(x)$  is infinite or  $\lim_{x \rightarrow a^+} f(x)$  is infinite

⇒ no vertical asymptote

fn is concave up  $\forall x$

